

Distribution Functions of Structural Heterogeneity of Microporous Adsorbents

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The distribution functions of structural heterogeneity of microporous adsorbents have been given. Influences of adsorbents and adsorbates types on this heterogeneity have been studied.

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Verteilungsfunktionen für die Struktur-Heterogenität von mikroporösen Adsorbentien

Es werden Verteilungsfunktionen für die strukturelle Heterogenität von mikroporösen Adsorbentien angegeben. Die Einflüsse der Adsorbens- und Adsorbatarten auf diese Heterogenität wurden untersucht.

Introduction

The theory of volume filling of micropores, proposed long ago by Dubinin [1], is described by two fundamental isotherm equations: the Dubinin-Astakhov (DA) [2] relationship and its special form—the Dubinin-Radushkevich (DR) equation. In 1965, Izotova and Dubinin [3] postulated that the DR equation can be applied only to solids of homogeneous micropore structure and they considered the case of an adsorbent of bimodal pore structure. Recently Stoeckli [4, 5] extended this approach using an integral equation describing the process of adsorption on solids with a continuous distribution of the micropores volume:

$$W(y) = \int_0^{\infty} f(B) \exp(-B \cdot y) dB \quad (1)$$

where W is the volume of a liquid-like adsorbate filling the micropores at temperature T and pressure p , B is the structural constant characterizing the solid, $f(B)$ is the distribution function of the micropores volume with respect to B , $y = (T/\beta)^2 \cdot \log^2(p_s/p)$, β is the constant characterizing the adsorbate (affinity coefficient), and p_s is the saturation pressure.

Expression (1) is an integral transform of the *Laplace* type, with the *DR* equation as the core equation. The function $f(B)$ can be described by various equations with known *Laplace* transform in order to obtain an analytical expression for the isotherm $W(y)$. *Stoekli* [4] used for $f(B)$ the *Gaussian* distribution as the first approximation and then he obtained the following adsorption isotherm (*DRS*):

$$W(y) = \frac{W_0}{2} \cdot \exp(-B_0 \cdot y) \exp\left(\frac{y^2 \Delta^2}{2}\right) [1 - \operatorname{erf}(x)] \quad (2)$$

where W_0 is the total volume of the micropores, B_0 and Δ represent the maximum and the half-width of the distribution function $f(B)$, $x = (y - B_0/\Delta^2) \cdot \Delta/\sqrt{2}$, and $\operatorname{erf}(x)$ is the error function.

Rozwadowski and *Wojasz* [6, 7] have examined Eq. (2) for many experimental adsorption isotherms of C_6H_6 , *MeOH*, *EtOH*, *MeNH_2*, *Me_2NH* and *EtNH_2* on carbons A, B, D and E at different temperatures. These data have been analyzed and, in spite of *Stoekli's* opinion [8], the applicability of the equation is limited to cases where $n \leq 2$ in the *DA* equation. Thus, a more general form of Eq. (1) is:

$$W(A) = \int_0^{\infty} f(k) \exp(-kA^n) dk \quad (1a)$$

where A is the differential molar work of adsorption, k is the structural constant characterizing the solid, and n is an integer constant; in the case when $n = 2$, then $k = B/(R \ln 10)^2$ and $A^2 = y(R \ln 10)^2$.

As zeolites and some active carbons have the parameter n greater than 2, the authors have derived [6] a more general isotherm equation which can be applied to all microporous solids.

$$W(A) = W_0 \exp\left[\frac{\Delta^2}{2} \left(\frac{A}{\beta}\right)^{2n}\right] \exp\left[-k_m \left(\frac{A}{\beta}\right)^n\right] \cdot \frac{\operatorname{erfc}\left[\frac{\Delta}{\sqrt{2}} \left(\frac{A}{\beta}\right)^n - \frac{k_m}{\Delta \sqrt{2}}\right]}{\operatorname{erfc}\left(-\frac{k_m}{\Delta \sqrt{2}}\right)} \quad (3)$$

where W_0 is the total normalized micropore volume, k_m represents the maximum of the distribution function of micropore volume with respect to k .

Eq. (3) allows to determine the texture parameters W_0 , k_m and Δ for all microporous adsorbents without any limitations, where Δ is the parameter characterizing the structural heterogeneity of microporous solids.

The aim of this paper is to determine the influences of microporous adsorbent texture and adsorbate type on the shape of the $f(k)$ function characterizing the distribution of micropores volume with respect to k . We want to show that, besides of the *Gaussian* distribution for the $f(B)$ function (Eq. 2), other $f(k)$ distributions—real from a physical point of view—are also possible to accept.

Theory

Stoeckli [4] introduced the distribution function of the microporous volume with respect to the parameter B . This distribution function $f(B)$ characterizes the heterogeneous micropore structure of the solid (structural heterogeneity). The *Gaussian* shape of $f(B)$ function assumed by *Stoeckli* is only one from many possible cases for the solution of integral Eq. (1) determining the global adsorption isotherm $W(y)$. The *Rayleigh* and exponential distributions are also real from a physical point of view. Moreover, *Stoeckli* has not included the normalization of the function $f(B)$, and according to our opinion [7], this may lead sometimes to values of W_0 which are out of physical sens. Thus, in relation to Eq. (3), the authors [6] have assumed the normalized *Gaussian* distribution function $f(k)$:

$$f(k) = \frac{2 W_0}{\Delta \sqrt{2 \pi} \cdot \operatorname{erfc}\left(-\frac{k_m}{\Delta \sqrt{2}}\right)} \cdot \exp\left[-\frac{(k-k_m)^2}{2 \Delta^2}\right] \quad k \geq 0$$

$$f(k) = 0 \quad k < 0 \quad (4)$$

In the next considerations only the normalized distributions have been used.

Assuming the *Rayleigh* distribution [9] (the *Gaussian* distribution with a widening at the right or left hand side) of $f(k)$ one should consider two cases:

a) the distribution with a widening at the right-hand side

$$f(k) = \frac{W_0}{\Delta^2} (k - k_0) \exp\left[-\frac{(k - k_0)}{2 \Delta^2}\right] \quad k_0 \geq 0 \text{ and } k \geq k_0$$

$$f(k) = 0 \quad k < k_0 \quad (5)$$

where k_0 is the parameter of the *Rayleigh* distribution and $k_0 = k_m - \Delta$.

Eq. (5) substituted into Eq. (1 a) gives

$$W = W_0 \exp \left[-k_0 \left(\frac{A}{\beta} \right)^n \right] \left\{ 1 - \sqrt{\frac{\pi}{2}} \cdot \Delta \cdot \left(\frac{A}{\beta} \right)^n \cdot \exp \left[\frac{\Delta^2}{2} \left(\frac{A}{\beta} \right)^{2n} \right] \cdot \operatorname{erfc} \left[\frac{\Delta}{\sqrt{2}} \left(\frac{A}{\beta} \right)^n \right] \right\} \quad (6)$$

b) the distribution with a widening at the left-hand side

$$f(k) = \frac{W_0(k_0 - k)}{\Delta^2 \left[1 - \exp \left(-\frac{k_0^2}{2\Delta^2} \right) \right]} \cdot \exp \left[-\frac{(k_0 - k)^2}{2\Delta^2} \right] \quad 0 \leq k \leq k_0 \quad (7)$$

$$f(k) = 0 \quad k > k_0 \quad \text{or} \quad k < 0$$

where $k_0 = k_m + \Delta$.

The substitution of (7) into Eq. (1 a) gives

$$W = \frac{W_0}{1 - \exp \left(-\frac{k_0^2}{2\Delta^2} \right)} \left\{ \exp \left[-k_0 \left(\frac{A}{\beta} \right)^n \right] + \left(\frac{A}{\beta} \right)^n \sqrt{\frac{\pi}{2}} \cdot \Delta \cdot \exp \left[-k_0 \left(\frac{A}{\beta} \right)^n \right] \cdot \exp \left[\frac{\Delta^2}{2} \left(\frac{A}{\beta} \right)^{2n} \right] \left[\operatorname{erfc} \left[\frac{\Delta}{\sqrt{2}} \left(\frac{A}{\beta} \right)^n - \frac{k_0}{\Delta \sqrt{2}} \right] - \operatorname{erfc} \left[\frac{\Delta}{\sqrt{2}} \left(\frac{A}{\beta} \right)^n \right] \right] - \exp \left(-\frac{k_0^2}{2\Delta^2} \right) \right\} \quad (8)$$

Assuming an exponential distribution of the $f(k)$ function one should consider also two cases:

a) the distribution for the decreasing exponential function $f(k)$

$$f(k) = \frac{W_0}{\Delta} \cdot \exp \left(-\frac{k - k_m}{\Delta} \right) \quad k_m \geq 0 \quad \text{and} \quad k \geq k_m \quad (9)$$

$$f(k) = 0 \quad k < k_m$$

The substitution of Eq. (9) into Eq. (1 a) leads to

$$W = \frac{W_0}{1 + \Delta \left(\frac{A}{\beta} \right)^n} \cdot \exp \left[-k_m \left(\frac{A}{\beta} \right)^n \right] \quad (10)$$

b) the distribution for the increasing exponential function $f(k)$

$$f(k) = \frac{W_0}{\Delta \left[1 - \exp\left(-\frac{k_m}{\Delta}\right) \right]} \cdot \exp\left(-\frac{k_m - k}{\Delta}\right) \quad 0 \leq k \leq k_m \quad (11)$$

$$f(k) = 0 \quad k > k_m \quad \text{or} \quad k < 0$$

Eq. (1 a) with the function (11) gives:

$$W = \frac{W_0 \left\{ \exp\left[-k_m \left(\frac{A}{\beta}\right)^n\right] - \exp\left(-\frac{k_m}{\Delta}\right) \right\}}{\left[1 - \Delta \left(\frac{A}{\beta}\right)^n \right] \left[1 - \exp\left(-\frac{k_m}{\Delta}\right) \right]} \quad A^n \neq 1/\Delta \quad (12)$$

$$W = \frac{W_0 k_0 \exp\left(-\frac{k_m}{\Delta}\right)}{\left[1 - \exp\left(-\frac{k_m}{\Delta}\right) \right]} \quad A^n = 1/\Delta$$

Experimental

The investigations have been made on active carbons prepared from chemically pure saccharose. The preparation method and texture of the carbons have been described previously [10–12]. The carbons have been activated with oxygen at 723 K (sample A), with carbon dioxide at 1 123 K (sample B) and also with ZnCl_2 in the process of so-called chemical activation (sample D and E). The adsorption isotherms for spectrally pure alcohols (methanol, ethanol) and for chemically pure aliphatic amines (MeNH_2 , Me_2NH and EtNH_2) have been measured within the temperature ranges 298.2–322.0 K and 298.2–335.7 K, respectively, using a *McBain* balance. The benzene adsorption isotherms have been measured at 298.2 K. In order to eliminate the irreversible adsorption in the case of amines, the adsorption process was investigated on carbons presaturated with the amines studied (the relative pressure of conditioning was about 0.2 and the temperature 298.2 K). After the equilibrium state reaching, the samples were desorbed under the pressure of 1 mPa at 335.7 K up to constant mass. Active carbons conditioned this way were next used to study amines adsorption. Examples of isotherms for the studied samples are shown in Figs. 1 and 2.

Results and Discussion

In accordance with considerations by many authors [13–15], there is a proportional dependence between the micropores radius (r_m) and the value of the B parameter in the DR equation

$$r_m = \text{const}_1 \cdot B^{1/2} \quad (13)$$

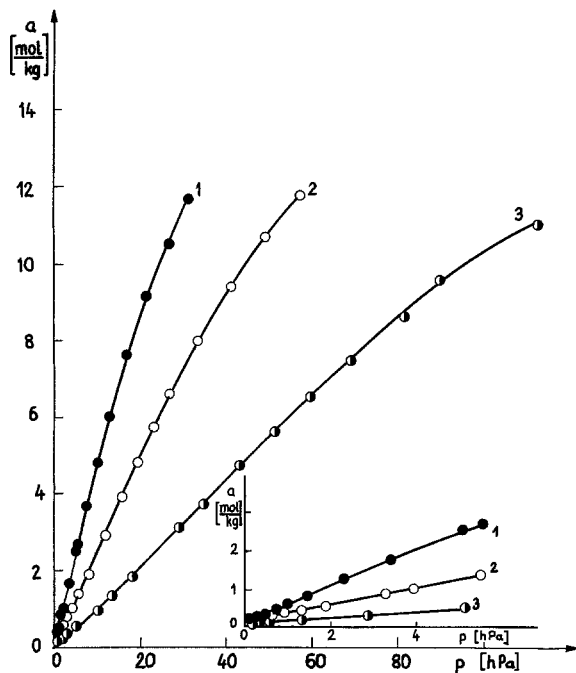


Fig. 1. Isotherms of *MeOH* adsorption on carbon D in the dependence on temperature: 1 298.2 K; 2 308.0 K; 3 322.7 K

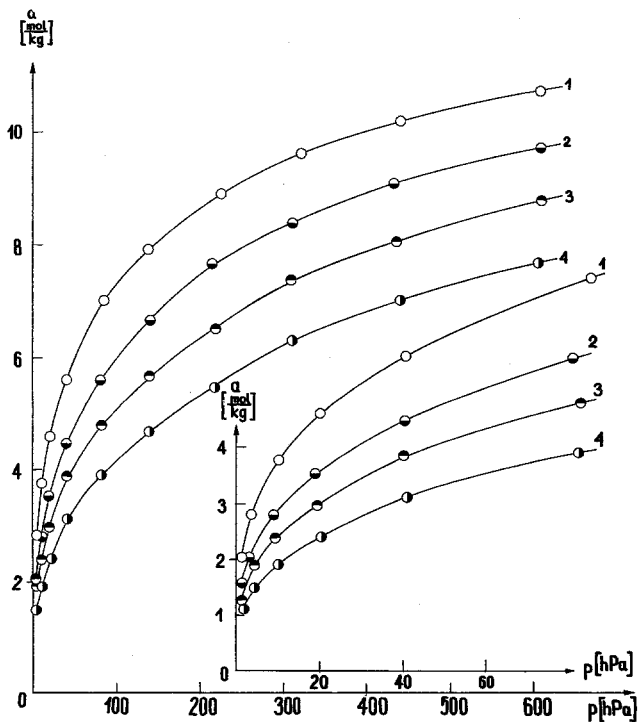


Fig. 2. Isotherms of *MeNH₂* adsorption on carbon B in the dependence on temperature: 1 298.2 K; 2 310.7 K; 3 323.2 K; 4 335.7 K

The same dependence occurs also between the r_m value and k in the other equations cited:

$$r_m = \text{const}_2 \cdot k^{1/2} \quad (14)$$

The value of the structural parameter k is changing within a definite range depending on values of r_m radii occurring in a given adsorbent. Thus, the value of the Δ parameter occurring in Eqs. (3)–(12) is a measure for changes of the micropores radii. Values of k_m , Δ and W_0 of above equations obtained with the method of the least-squares for all cases studied are listed in Table 1 a–1 c.

Table 1 a. Parameters of the distribution functions of structural heterogeneity for adsorption systems studied

$$* \left([k] = [k_m] = [\Delta] = \left[\frac{\text{mol}^n}{\text{kJ}^n} \right], [f(k_m)] = \left[\frac{\text{kJ}^n \text{ dm}^3}{\text{mol}^n \text{ kg}} \right], [W_0] = \left[\frac{\text{dm}^3}{\text{kg}} \right]; \right. \\ \left. k \in \langle k_{\text{from}}, k_{\text{to}} \rangle \Rightarrow f(k) \geq 0.01 \cdot f(k_m) \right)$$

Adsorbent	Adsorbate	DA		Eq. (3)					
		n	k $\times 10^6$	Range of k $\times 10^6$		k_m $\times 10^6$	$f(k_m)$	Δ $\times 10^6$	W_0
				from	to				
A	MeOH	3	57.9	0	186	71.8	2 630	37.7	0.2413
B		2	3 427	0	11 360	5 290	169.2	2 005	0.8467
D		2	3 799	0	16 200	7 149	123.0	2 990	0.9141
E	EtOH	2	3 352	0	18 600	7 357	61.38	3 696	0.5524
A		3	58.2	0	223	72.2	1 992	49.6	0.2297
B		2	3 258	190	7 680	3 953	223.4	1 266	0.6865
D		2	3 927	0	14 400	6 474	133.4	2 594	0.8621
E		2	3 699	0	21 010	8 229	65.17	4 198	0.6686
A	MeNH ₂	2	481.9	0	1 042	521.6	577.0	173.2	0.2504
B		2	861.1	0	4 668	1 334	242.7	1 098	0.5931
D		2	896.3	0	7 284	1 431	185.1	1 937	0.6920
E		2	788.3	0	5 879	1 489	149.9	1 481	0.4587
A	Me ₂ NH	2	672.2	272	1 092	683.9	675.0	132.4	0.2240
B		2	1 318	0	3 156	1 496	410.1	548.3	0.5619
D		2	1 517	0	6 970	2 123	187.1	1 602	0.6817
E		2	1 559	0	7 935	2 501	137.9	1 786	0.5675
A		EtNH ₂	2	742.9	0	2 972	662.5	139.0	139.0
B	2		1 357	0	3 668	1 587	314.1	686.0	0.5345
D	2		1 539	0	7 851	2 041	164.7	1 913	0.6767
E	2		1 482	0	9 803	2 219	118.2	2 502	0.6021
A	C ₆ H ₆	3	54.5	0	179	71.5	2 389	35.3	0.2069
B		2	2 393	2 080	2 720	2 399	2 240	103.0	0.5761
D		2	2 916	0	8 100	3 937	196.0	1 370	0.6714
E		2	2 823	0	11 200	4 690	97.21	2 148	0.5158

Table 1 b. Parameters of the distribution functions of structural

Adsorbent	Adsorbate	Eq. (6)					
		Range of k $\times 10^6$		k_m $\times 10^6$	$f(k_m)$	Δ $\times 10^6$	W_0
		from	to				
A	MeOH	1.52	213	60.7	2480	59.2	0.2421
B		613.7	16080	4942	128.3	4327	0.9160
D		233.8	25200	7228	94.23	6994	1.0866
E		0	26700	7207	51.37	7568	0.6402
A	EtOH	0	243	61.9	1994	70.5	0.2300
B		1218	9320	3487	184.9	2269	0.6917
D		460.6	20340	6026	100.7	5563	0.9241
E		0	28720	7722	54.24	8163	0.7290
A	MeNH ₂	161.2	1206	453.4	520.7	292.2	0.2508
B		0	5187	1163	239.9	1561	0.5978
D		0	7850	1294	187.2	2548	0.6967
E		0	6440	1228	149.9	2033	0.4646
A	Me ₂ NH	416.1	1184	630.6	633.5	214.5	0.2240
B		351.7	3682	1288	365.2	936.2	0.5636
D		0	7715	1838	185.5	2283	0.6850
E		0	8987	2171	134.1	2636	0.5740
A	EtNH ₂	0	3083	610.6	144.3	960.4	0.2138
B		219.8	4214	1344	289.0	1124	0.5357
D		0	8472	1798	166.4	2595	0.6791
E		0	10690	1983	118.9	3377	0.6080
A	C ₆ H ₆	2.95	208	60.3	2193	57.3	0.2073
B		2215	2730	2360	2404	145.3	0.5758
D		762.0	10600	3509	151.7	2747	0.6871
E		87.24	14700	4180	79.07	4092	0.5335

As it can be seen from the data presented in the Table 1 a–1 c, the values of Δ and k_m from Eqs. (3), (6), (8), (10), and (12) increase for carbons studied in sequence A, B, D, E. Parameter k_m , similarly like B or k in the DR equation can be employed as an indication for the adsorption potential. The lower the values of k_m , the greater is the adsorption potential of the micropore system. At the same time, in the case of carbon of strongly increased adsorption potential (sample A), the heterogeneity parameter Δ usually has a low value. It results from Eq. (14) that the distribution of the micropores sizes becomes broader with an increase of Δ . This means (Table 1 a–1 c) that carbon E has the best developed system

heterogeneity for adsorption systems studied* (as in Table 1a)

Eq. (8)					
Range of k $\times 10^6$		k_m $\times 10^6$	$f(k_m)$	Δ $\times 10^6$	W_0
from	to				
0	141	83.2	2649	58.1	0.2407
0	8367	5730	191.2	2636	0.8259
0	11530	7665	138.8	3864	0.8736
0	12800	7970	67.69	4870	0.5266
0	167	85.1	1935	82.3	0.2293
30	5990	4318	248.3	1672	0.6835
0	10470	7052	151.0	3422	0.8440
0	14650	9039	72.12	5608	0.6450
0	831.9	580.7	606.8	251.1	0.2502
0	3350	1574	241.1	1775	0.5868
0	5053	1658	180.9	3396	0.6780
0	4048	1618	148.5	2430	0.4464
232	923.7	731.8	707.5	192.0	0.2240
0	2469	1676	432.4	793.1	0.5610
0	5105	2502	184.8	2603	0.6773
0	5664	2915	140.1	2748	0.5586
0	2273	657.2	127.5	1616	0.2135
0	2840	1811	321.8	1028.8	0.5338
0	5722	2394	158.7	3328	0.6723
0	6884	2581	115.3	4304	0.5905
0	135	82.4	2464	52.8	0.2066
2010	2610	2443	2071	168.6	0.5760
0	6140	4301	221.0	1834	0.6658
0	8140	5214	107.7	2926	0.5085

of micropores of different sizes. On the other hand, carbon A with the most increased adsorption potential has a relatively homogeneous system of micropores. One can then accept that the Δ parameter from Eqs. (3)–(12) characterizes the structural heterogeneity of microporous adsorbents.

Examples for the functions of the adsorption energy distribution obtained from Eqs. (3), (6), (8), (10), (12), and (DR) are shown in Figs. 3–4.

It should be stated that, in spite of assumed differences in the shape of the $f(k)$ functions, the distribution curves obtained from those equations contain a broad common range of k values.

Table 1 c. *Parameters of the distribution functions of structural*

Adsorbent	Adsorbate	Eq. (10)					
		Range of k $\times 10^6$ from to		k_m $\times 10^6$	$f(k_m)$	Δ $\times 10^6$	W_0
A	MeOH	25.9	281.4	25.9	4413	55.5	0.2449
B		1 731	41 250	1 731	140.8	8 582	1.2083
D		1 552	334 300	1 552	73.80	70 760	5.2220
E		1 024	5 652 500	1 024	37.66	1 227 200	46.215
A	EtOH	20.7	328	20.7	3 486	66.6	0.2322
B		2 116	12 220	2 116	319.7	2 192	0.7010
D		1 796	53 230	1 796	106.8	11 170	1.1923
E		1 132	178 330	1 132	44.47	38 480	1.7113
A	MeNH ₂	296.3	1 422	296.3	1 030.4	244.4	0.2518
B		220.8	9 233	220.8	332.1	1 957	0.6500
D		145.0	14 930	145.0	247.8	3 211	0.7956
E		138.8	14 960	138.8	183.6	3 217	0.5905
A	Me ₂ NH	527.5	1 263	527.5	1 403.4	159.7	0.2241
B		763.7	4 559	763.7	688.9	824.0	0.5676
D		451.0	12 270	451.0	279.0	2 571	0.7173
E		438.8	18 190	438.8	171.9	3 862	0.6638
A	EtNH ₂	217.2	3 637	217.2	289.8	740.6	0.2146
B		724.5	5 167	724.5	557.7	965.2	0.5383
D		393.2	13 040	393.2	257.4	2 752	0.7084
E		280.1	20 490	280.1	159.7	4 399	0.7022
A	C ₆ H ₆	24.7	284	24.7	3 709	56.4	0.2090
B		2 290	2 800	2 290	5 260	109	0.5759
D		1 623	17 600	1 623	209.8	3 478	0.7298
E		1 117	31 900	1 117	89.42	6 954	0.6218

If assumed that the *Dirac's* function resulting from the *DR* equation describes the position of maximum of distribution function $f(k)$ most exactly, then Eq. (5) gives the most correct distribution of adsorption energy. On the other hand, Eq. (11) gives the position of the maximum most departing from that assumed in the *DR* equation. It can be also stated that the distribution function $f(k)$ resulting from Eq. (9), contains always the broadest range of k values. If the range of changes of the k values is accepted as a criterion of the applicability of these functions then Eq. (9) should be excluded since it gives results most departing from the other functions of adsorption energy distribution. Besides of that, it

heterogeneity for adsorption systems studied* (as in Table 1 a)

Eq. (12)					
Range of k $\times 10^6$		k_m $\times 10^6$	$f(k_m)$	Δ $\times 10^6$	W_0
from	to				
0	113	113	4 666	61.2	0.2402
0	6 348	6 348	503.1	1 623	0.8003
0	8 404	8 404	354.7	69 570	0.8222
0	9 128	9 128	154.0	3 428	0.4910
0	132.8	132.8	2 769	128.1	0.2289
90	4 812	4 812	670.2	1 023	0.6793
0	7 867	7 867	394.3	2 134	0.8203
0	10 525	10 525	165.4	4 008	0.6148
0	683.8	683.8	1 391.1	184.2	0.2499
0	2 549	2 549	345.0	2 847	0.5809
0	3 824	3 824	196.9	16 208	0.6707
0	2 977	2 977	191.2	5 279	0.4351
250	800.3	800.3	1 880.5	119.2	0.2239
0	2 003	2 003	967.4	600.2	0.5600
0	3 951	3 951	267.7	4 019	0.6734
0	4 282	4 282	223.8	3 465	0.5501
0	1 392	1 392	264.7	1 119	0.2108
0	2 290	2 290	636.3	911.6	0.5330
0	4 439	4 439	194.5	8 297	0.6687
0	5 183	5 183	136.4	12 792	0.5813
0	107.1	107.1	4 729	49.2	0.2063
2020	2 503	2 503	5 580	103	0.5759
0	4 798	4 798	595.4	1 122	0.6585
0	6 117	6 117	254.7	2 069	0.4995

results from data presented in Table 1 a–1 c as well as partially in Figs. 3–4 that the shape and values of the function of adsorption energy distribution depend also on the type of molecules adsorbed. Considering an increase of k_m values, the examined adsorbates can be most often placed in the order: $MeNH_2 < Me_2NH \approx EtNH_2 < C_6H_6 < MeOH \approx EtOH$. The parameter Δ on the other hand is increasing in the following order: $C_6H_6, MeNH_2, Me_2NH, EtNH_2 < MeOH, EtOH$. It should be expected that the values of k_m and Δ are influenced not only by the dimensions of adsorbed molecules and adsorbent texture but also by adsorbate-adsorbate and adsorbate-adsorbent interactions.

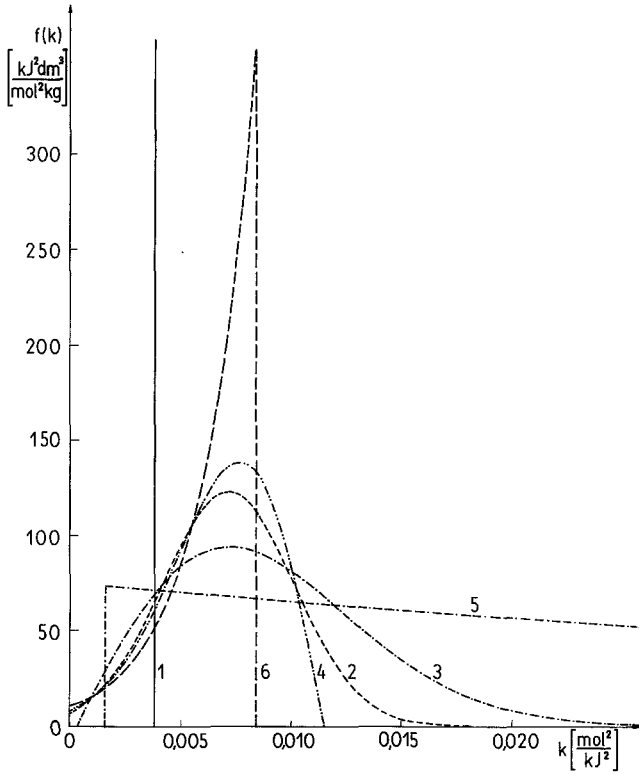


Fig. 3. Functions of the structural parameter distribution for *MeOH* adsorption on carbon D: 1 the distribution resulting from the *DR* equation; 2 the distribution resulting from Eq. (3) described with Eq. (4); 3 the distribution resulting from Eq. (6) described with Eq. (5); 4 the distribution resulting from Eq. (8) described with Eq. (7); 5 the distribution resulting from Eq. (10) described with Eq. (9); 6 the distribution resulting from Eq. (12) described with Eq. (11)

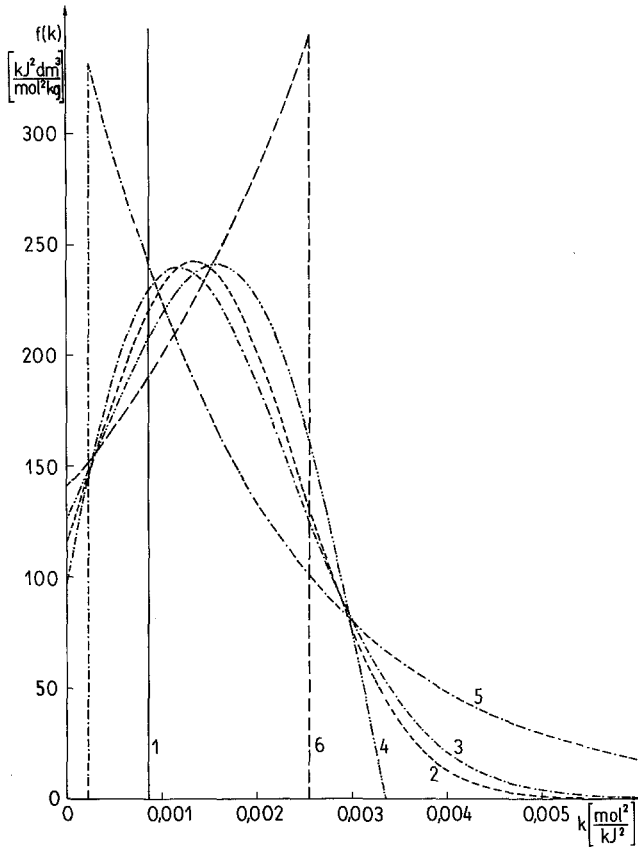


Fig. 4. Functions of the structural parameter distribution for $MeNH_2$ adsorption on the carbon B: 1 the distribution resulting from the DR equation; 2 the distribution resulting from Eq. (3) described with Eq. (4); 3 the distribution resulting from Eq. (6) described with Eq. (5); 4 the distribution resulting from Eq. (8) described with Eq. (7); 5 the distribution resulting from Eq. (10) described with Eq. (9); 6 the distribution resulting from Eq. (12) described with Eq. (11)

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